

GRAPHING SINE AND COSINE FUNCTIONS QUIZ

1. Determine the amplitude of $y = -2\cos x - 3$

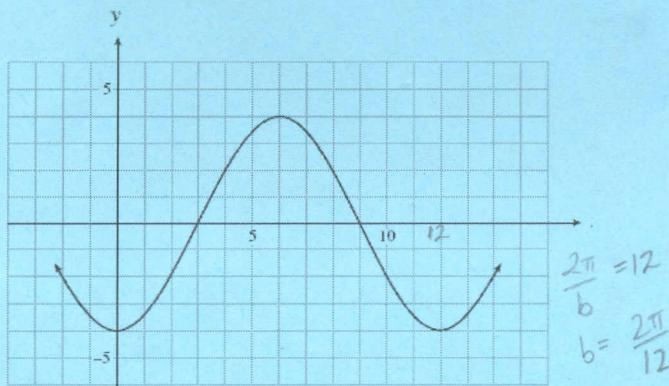
(a) -3

(b) -2

(c) 2

(d) 3

2. Given the graph below, determine an equation of this function.



$$(a) y = -4\cos \frac{\pi}{6}x$$

$$(b) y = 4\cos \frac{\pi}{6}x$$

$$(c) y = -4\cos \frac{\pi}{12}x$$

$$(d) y = 4\cos \frac{\pi}{12}x$$

3. List the vertical shift, amplitude, phase shift and period for each function, and sketch the graph, setting the vertical scale and the horizontal scale.

(a) $y = 3\sin(2\theta)$

vertical shift:

0

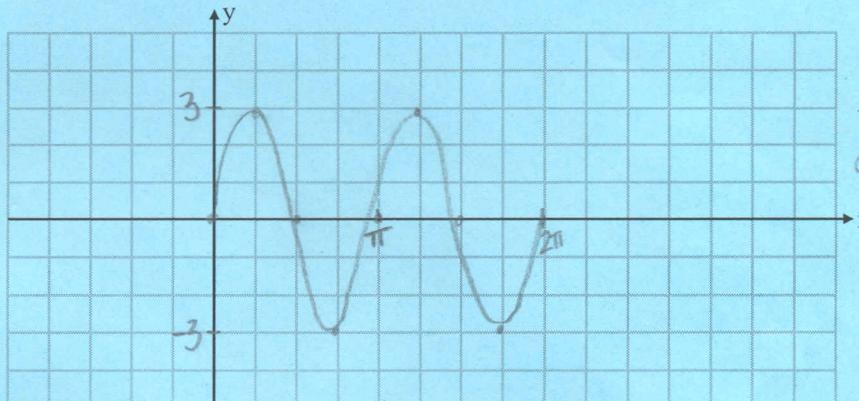
amplitude:

3

phase shift:

0

period:

π

0.5 V.S.
0.5 H.S.

marking scheme:

0-1 correct → 0

2-3 correct → 0.5

4 correct → 1

(b) $y = 2\cos 3(\theta - \frac{\pi}{2}) + 3$

vertical shift:

3

amplitude:

2

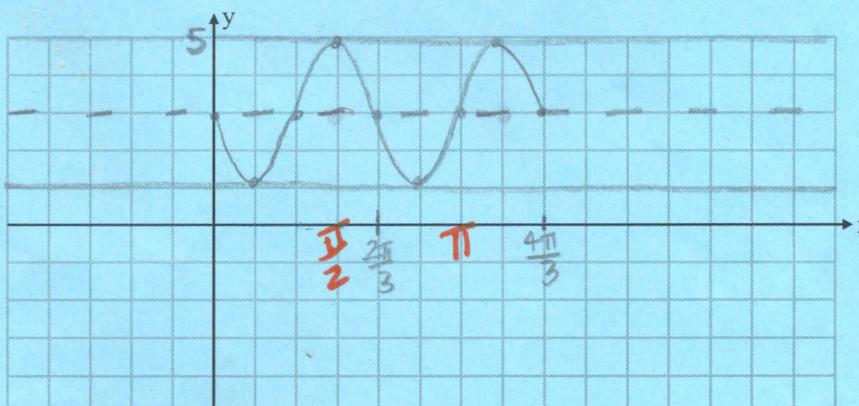
phase shift:

π/2

period:

2π/3

intervals: $\frac{2π/3}{4} = \frac{π}{6}$

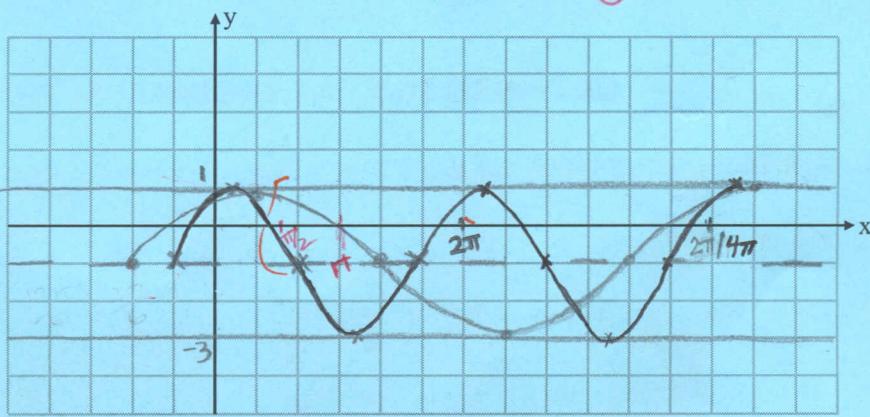


$$(c) y = 2\sin(\theta + \frac{\pi}{3}) - 1$$

vertical shift: $\underline{-1}$
 amplitude: $\underline{2}$
 phase shift: $\underline{-\frac{\pi}{3}} = \underline{-\frac{2\pi}{6}}$
 period: $\underline{2\pi}$

$$\text{intervals: } \frac{2\pi}{4} = \frac{\pi}{2} = \frac{3\pi}{6}$$

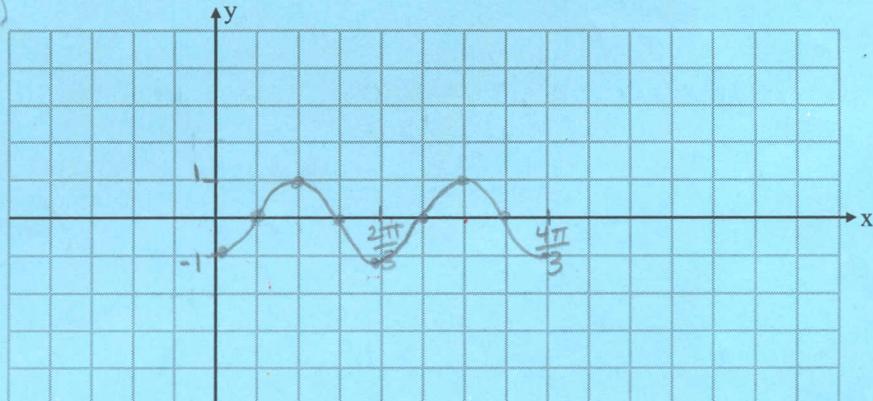
OR last point: $-\frac{\pi}{3} + 2\pi = \frac{5\pi}{3}$



$$(d) y = \sin(3\theta - \frac{\pi}{2}) = \sin 3(\theta - \frac{\pi}{6})$$

vertical shift: $\underline{0}$
 amplitude: $\underline{1}$
 phase shift: $\underline{\frac{\pi}{6}}$
 period: $\underline{\frac{2\pi}{3}} = \underline{4\pi/6}$

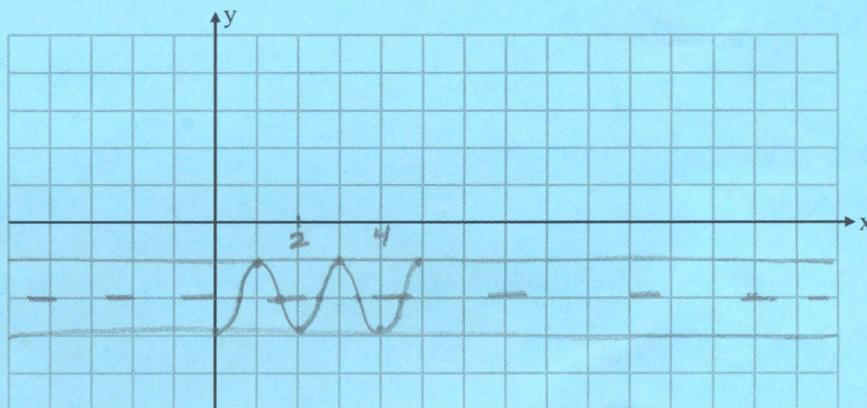
$$\text{intervals: } \frac{2\pi}{3} \div 4 = \frac{2\pi}{12} = \frac{\pi}{6}$$



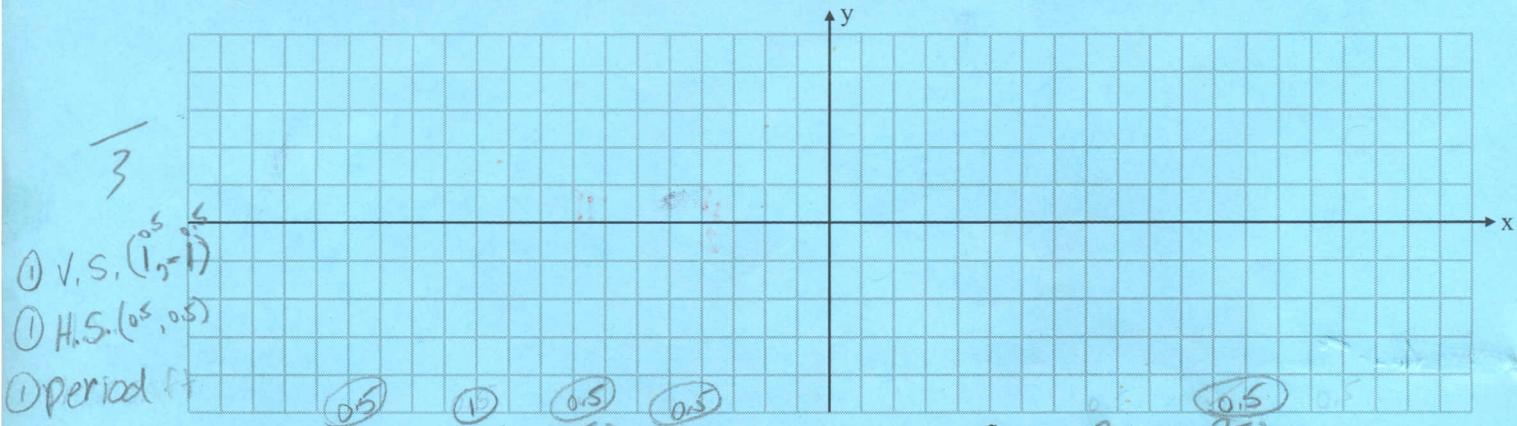
$$(e) y = \cos\pi(t-1) - 2$$

vertical shift: $\underline{-2}$
 amplitude: $\underline{1}$
 phase shift: $\underline{1}$
 period: $\underline{2}$

$$\text{intervals: } \frac{2}{4} = \frac{1}{2}$$



4. The following graph represents a COSINE function. State 2 possible COSINE equations.



$$(a) \underline{1 \cos 2(\theta + \frac{\pi}{4}) - 1}$$

$$(b) \underline{1 \cos 2(\theta - \frac{3\pi}{4}) - 1}$$

$$\text{Period: } \frac{14\pi}{8} - \frac{6\pi}{8} = \frac{8\pi}{8} = \pi$$

$$\frac{2\pi}{b} = \pi \quad b = 2$$

$$2\cos 2(\theta + \frac{5\pi}{4}) - 1$$

$$2\cos 2(\theta + \frac{9\pi}{4}) - 1$$

$$\underline{1 \cos 2(\theta - \frac{\pi}{4}) - 1}$$

$$\underline{-\cos 2(\theta - \frac{3\pi}{4}) - 1}$$