

MATH 12 QUIZ : TRIG EQUATIONS

NAME _____

DATE _____

BLOCK _____

1) Solve algebraically over the real numbers. (Find the general solution with exact values)

$$2\cos^2 x + \cos x - 1 = 0$$

2) Find all values of x *exactly*, where $0 < x < 2\pi$ which solve the equation:

$$\tan x + 1 = \sec^2 x$$

$x =$ _____
3) Solve for x to the nearest hundredth, where $0 \leq x < 2\pi$

$$3\sin x - 2\csc x = 5$$

$x =$ _____
4) Solve for x exactly over the real numbers:

$$4\sin x \cos x = -\sqrt{3}$$

$x =$ _____

$x =$ _____

5) Find all values of x , in general form, for which the expression:

$$\frac{\csc x}{\csc x - 1} \text{ Is undefined}$$

6) Solve : $\sec\theta + \cot\theta = 2$, $0 < \theta < 2\pi$

$$x = \underline{\hspace{2cm}}$$

A. 0.64

B. 0.93

C. 3.46, 5.13

D. 4.29, 5.97

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1) Solve algebraically over the real numbers. (Find the general solution with exact values)

$$2\cos^2 x + \cos x - 1 = 0$$

$$\begin{aligned} (2\cos x - 1)(\cos x + 1) &= 0 \\ \cos x &= 1/2 \quad \cos x = -1 \\ x &= \pi/3, 5\pi/3 \quad x = \pi \end{aligned}$$

$$x = \frac{\pi}{3} + 2\pi n, \frac{5\pi}{3} + 2\pi n, \pi + 2\pi n$$

3) Solve for x to the nearest hundredth, where $0 \leq x < 2\pi$

$$3\sin x - 2\csc x = 5$$

$$3\sin x - \frac{2}{\sin x} = 5$$

$$3\sin^2 x - 2 = 5\sin x$$

$$3\sin^2 x - 5\sin x - 2 = 0$$

$$(3\sin x + 1)(\sin x - 2) = 0$$

$$\sin x = -1/3 \quad \sin x = 2$$

$$x = \sin^{-1}(-1/3) \quad \text{too big!}$$

$$x = -0.340$$

$$2\pi - 0.340 = 5.94$$

$$\pi + 0.340 = 3.48$$

$$x = 3.48, 5.94$$

2) Find all values of x exactly, where $0 < x < 2\pi$ which solve the equation:

$$\tan x + 1 = \sec^2 x$$

$$\tan x + 1 = 1 + \tan^2 x$$

$$\tan^2 x - \tan x = 0$$

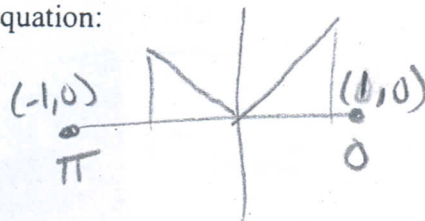
$$\tan x(\tan x - 1) = 0$$

$$\tan x = 0$$

$$x = 0, \pi$$

$$\tan x = 1$$

$$x = \pi/4, 5\pi/4$$



$$\tan = \frac{y}{x} = \frac{\sin}{\cos}$$

$$x =$$

4) Solve for x exactly over the real numbers:

$$4\sin x \cos x = -\sqrt{3}$$

$$2(2\sin x \cos x) = -\sqrt{3}$$

$$2\sin 2x = -\sqrt{3}$$

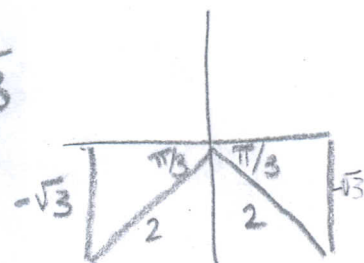
$$\sin 2x = -\sqrt{3}/2$$

$$2x = \sin^{-1}(-\sqrt{3}/2)$$

$$2x = \pi + \frac{\pi}{3} = \frac{4\pi}{3} \quad x = \frac{4\pi}{6} = \frac{2\pi}{3}$$

$$2x = 2\pi - \frac{\pi}{3} = \frac{5\pi}{3} \quad x = \frac{5\pi}{6}$$

$$x = \frac{2\pi}{3} + \pi n \quad x = \frac{5\pi}{6} + \pi n$$



$$x = \frac{2\pi}{3} + \pi n, \frac{5\pi}{6} + \pi n$$

5) Find all values of x , in general form, for which the expression:

$\frac{\csc x}{\csc x - 1}$ Is undefined

$$\frac{\frac{1}{\sin x}}{\frac{1}{\sin x} - 1}$$

Denominators = 0

$$\sin x = 0$$

$$x = 0, \pi, 2\pi$$

$$= \pi n$$

$$\frac{1}{\sin x} - 1 = 0$$

$$\frac{1}{\sin x} = 1$$

$$\sin x = 1$$

$$x = \frac{\pi}{2} + 2\pi n$$

6) Solve : $\sec \theta + \cot \theta = 2$, $0 < \theta < 2\pi$

A. 0.64

B. 0.93

C. 3.46, 5.13

D. 4.29, 5.97

$$x = \frac{\pi n, \pi/2 + 2\pi n}{2}$$

$$\text{or } \frac{\pi}{2} + \pi n$$

Graphing Calc.

$$y_1 = 1/\cos x + 1/\tan x$$

$$y_2 = 2$$